MULTIMEDIA UNIVERSITY

FINAL EXAMINATION

TRIMESTER 1, 2018/2019

BST1034 – STATISTICS FOR MANAGERS
(All sections / Groups)

27 OCTOBER 2018
9:00 a.m. – 11:00 a.m.
(2 Hours)

INSTRUCTIONS TO STUDENT

1. This question paper consists of **8** printed pages excluding the cover page, with **4** questions only.

2. Attempt **ALL** the questions. All questions carry equal marks and the distribution of the marks for each question is given.

3. Students are allowed to use non-programmable scientific calculators (without restriction).

4. All necessary workings must be shown and please write all your answers in the answer booklet provided.

QUESTION 1

a)   The following is the total amount (in RM) spent on mobile apps per year of a random sample of 100 Multimedia University's students.

Amount Spent (RM)	Number of Students
0-20	16
20-40	33
40-60	20
60-80	15
80-100	9
100-120	7

(i)   Compute mean and median of the data set.

(6 marks)

(ii)   Calculate the standard deviation and coefficient of variation of the data set.

(6 marks)

b)   The owner of a western food restaurant would like to study the paying methods of its customers. According to the data collected, 60% of its customers paid their bills by credit card. For customers who paid by card, 80% of the bill exceed RM50, and for customers who paid by cash, 70% of the bill is not more than RM50.

(i)   Find the probability that the bill is more than RM50.

(2 marks)

(ii)   If the bill is more than RM50, what is the probability that it will be paid by cash?

(3 marks)

c)   A research has shown that consumers spend an average of RM30 per week in cash without being aware of where it goes. Assume that amount of cash spent without being aware of where it goes is normally distributed and that the standard deviation is RM6.

(i)   What is the probability that a randomly selected person will spend between RM 20 and RM 35 per week?   (4 marks)

(ii)   What is the amount that only 1% of the consumers spent more than this amount?

(4 marks)

(Total: 25 marks)

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QUESTION 2

a) In the year 2017, a program has been conducted to help students who are under probation to improve their CGPA. A random sample of 10 students who had participated in the program was selected and their CGPA is given as follows:

$$2.10 \quad 2.20 \quad 2.00 \quad 2.56 \quad 2.87$$
$$2.35 \quad 2.11 \quad 2.90 \quad 2.66 \quad 2.55$$

    (i)   Construct a 95% confidence interval for the mean CGPA of probation students.

(6 marks)

    (ii)   Based on the ERU's record, the mean CGPA of probation students was 2.2. Test if the mean CGPA of probation students has increased after the program at 5% significance level.

(8 marks)

b) The Dean of the Faculty of Business would like to know is there a difference in the proportion of probation students between Marketing and Accounting programmes. To test this, 50 Marketing students and 75 Accounting students are selected and their academic status is recorded. Of those selected, 5 Marketing and 8 Accounting students are under probation. Test at the 5% significance level whether the proportions of Marketing and Accounting students who are under probation are different.

(11 marks)

(Total: 25 Marks)

Continued...

QUESTION 3

a) A marketing company is currently preparing an advertisement for a product. Three advertisements have been prepared. A random sample of 45 adults was selected and randomly assigned to the three advertisements. After reading the advertisement, they were asked to rate the advertisement from 1-10. A study was conducted to test is there a difference in rating for the three advertisements and the result is shown as follows,

SUMMARY

Advertisement	Count	Sum	Average	Variance
A	15	110	7.3333	8.3244
B	15	108	7.2	16.5577
C	15	115	7.6667	12.3333

ANOVA

Source of Variation	SS	df	MS	F
Between Groups		2		
Within Groups				
Total	522.7493	44		

(i) Complete the ANOVA table.

(7 marks)

(ii) Test at the 2.5% significance level to determine whether the mean rating of the three advertisements differ.

(6 marks)

b) The following data has been collected to determine if there a relationship between student's faculty and student's CGPA classification.

		CGPA Classification			
	First class	Second upper	Second lower	Third class	Total
FOB	40	97	133	30	300
FOL	18	25	32	25	100
FET	22	28	35	15	100
Total	80	150	200	70	500

Is there evidence that there is a relationship between student's faculty and student's CGPA classification? Test using the 1% level of significance.

(12 marks)

(Total: 25 marks)

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QUESTION 4

a) Research has shown that the number of hours spent on mobile games per day is one of the factors that would affect students' CGPA. The CGPA of 12 students and their time spent on mobile games per day is as follow:

Hours spent on mobile games	1	3	5	0.5	2	2	1	0.5	3	3	1	4
Student's CGPA	3.5	3.0	2.5	3.8	3.3	3.1	3.6	3.8	2.8	2.9	3.2	2.4

(i) Compute the coefficient of correlation and coefficient of determination.

(4 marks)

(ii) Determine the equation of the regression line.

(7 marks)

(iii) Estimate the student's CGPA if he spent 5 hours per day on mobile games. Is this estimation reliable?

(2 marks)

b) The computer output shown below is obtained from a regression model. The regression model consists of 1 dependent variable and 3 independent variables.

Dependent variable: Student's CGPA

Independent variable: Hours spent on mobile games per day, hours spent on social media, and hours used in revision before an exam.

ANOVA

	df	SS	MS	F
Regression				
Residual	26	100.2323		
Total	29	510.5155		

	Coefficient	t-Stat
Intercept	0.5133	5.2333
Hours spent on Mobile games	-1.233	1.4233
Hours spent on social media	-0.8333	2.113
Hours used in revision	1.3275	2.5849

(i) Complete the ANOVA table.

(4 marks)

(ii) Test the regression coefficients individually. Would you consider omitting any variables? If so, which one? Use the 0.05 significance level.

(8 marks)

(Total: 25 Marks)

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APPENDIXES:
I. STATISTICAL FORMULAE

A. DESCRIPTIVE STATISTICS

Ungrouped Data:

Sample Mean, $\bar{x} = \dfrac{\sum x}{n}$ Sample Standard Deviation, $s = \sqrt{\dfrac{\sum x^2}{n-1} - \dfrac{(\sum x)^2}{n(n-1)}}$

Grouped Data:

Sample Mean, $\bar{x} = \dfrac{\sum fx}{\sum f}$ Sample Standard Deviation, $s = \sqrt{\dfrac{\sum fx^2}{\sum f - 1} - \dfrac{(\sum fx)^2}{\sum f(\sum f - 1)}}$

$$\text{Median} = L_m + \left[\dfrac{\left(\dfrac{\sum f}{2} - F_{m-1}\right)}{f_m}\right]c \qquad \text{Mode} = L_m + \left[\dfrac{(f_m - f_{m-1})}{2f_m - f_{m-1} - f_{m+1}}\right]c$$

B. PROBABILITY DISTRIBUTION

Poisson Probability Distribution

If X follows a Poisson Distribution P (λ) where $P(X = x) = \dfrac{\lambda^x e^{-\lambda}}{x!}$

then the mean = $E(X) = \lambda$ and variance = $VAR(X) = \lambda$

Binomial Probability Distribution

If X follows a Binomial Distribution B(n, p) where $P(X = x) = {}^nC_x p^x q^{n-x}$

then the mean = $E(X) = np$ and variance = $VAR(X) = npq$ where $q = 1-p$

Normal Distribution

If $X \sim N(\mu, \sigma)$ where $E(X) = \mu$ and $VAR(X) = \sigma^2$, then $Z = \dfrac{X - \mu}{\sigma}$

C. CONFIDENCE INTERVAL ESTIMATION AND SAMPLE SIZE DETERMINATION

If σ known, $(100-\alpha)\%$ Confidence Interval for Population Mean, μ: $\bar{x} \pm Z_{\alpha/2} \dfrac{\sigma}{\sqrt{n}}$

If σ unknown, $(100-\alpha)\%$ Confidence Interval for Population Mean, μ: $\bar{x} \pm t_{\alpha/2, n-1} \dfrac{s}{\sqrt{n}}$

$(100-\alpha)\%$ Confidence Interval for Population Proportion, π: $p \pm Z_{\alpha/2} \sqrt{\dfrac{p(1-p)}{n}}$

Sample Size Determination for Population Mean: $n = \dfrac{(Z_{\alpha/2})^2 \sigma^2}{E^2}$

Sample Size Determination for Population Proportion: $n = \dfrac{(Z_{\alpha/2})^2 p(1-p)}{E^2}$

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D. HYPOTHESIS TESTING

One Sample Mean Test

Z-test: $Z = \dfrac{\bar{x} - \mu}{\dfrac{\sigma}{\sqrt{n}}}$ t-test: $t = \dfrac{\bar{x} - \mu}{\dfrac{s}{\sqrt{n}}}$

One Sample Proportion Test

$Z = \dfrac{p - \pi}{\sqrt{\dfrac{\pi(1 - \pi)}{n}}}$

Two Sample Mean Test

Z-test: $Z = \dfrac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{\sqrt{\dfrac{\sigma_1^2}{n_1} + \dfrac{\sigma_2^2}{n_2}}}$

t-test: $t = \dfrac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{s_p\sqrt{\left(\dfrac{1}{n_1} + \dfrac{1}{n_2}\right)}}$ where $s_p = \sqrt{\dfrac{(n_1 - 1)s_1^2 + (n_2 - 1)s_2^2}{n_1 + n_2 - 2}}$

Two Sample Proportion Test

$Z = \dfrac{(p_1 - p_2) - (\pi_1 - \pi_2)}{\sqrt{\bar{p}(1 - \bar{p})\left[\dfrac{1}{n_1} + \dfrac{1}{n_2}\right]}}$ where $= \bar{p} = \dfrac{x_1 + x_2}{n_1 + n_2}$

E. ANALYSIS OF VARIANCE

$$SST = \sum_{i=1}^{k}\sum_{j=1}^{n_j}\left(X_{ij} - \bar{\bar{X}}\right)^2 \qquad SSB = \sum_{i=1}^{k} n_i\left(\bar{X}_i - \bar{\bar{X}}\right)^2$$

$$SSW = \sum_{i=1}^{k}(n_i - 1)s_i^2 \qquad \text{or} \qquad SSW = \sum_{i=1}^{k}\sum_{j=1}^{n_j}\left(x_{ij} - \bar{x}_i\right)^2$$

F. CHI-SQUARE ANALYSIS

Expected cell frequencies for Independent Test: $E_i = \dfrac{Row\ total \times Column\ total}{N}$

Chi-Square test statistic: $\chi^2 = \sum \dfrac{(O_i - E_i)^2}{E_i}$

O_i = Observed frequency in a particular cell

E_i = expected frequency in a particular cell

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G. REGRESSION ANALYSIS

Correlation Coefficient: $r = \dfrac{n\sum xy - \sum x \sum y}{\sqrt{[n\sum x^2 - (\sum x)^2][n\sum y^2 - (\sum y)^2]}}$

Simple Linear Regression: $Y = a + bX$ where $b = \dfrac{\sum xy - \dfrac{\sum x \sum y}{n}}{\sum x^2 - \dfrac{(\sum x)^2}{n}}$ and

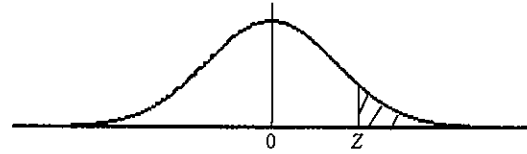$a = \bar{y} - b\bar{x}$

H. INDEX NUMBERS

Simple Price Index	Laspeyres Quantity Index
$P = \dfrac{p_t}{p_0} \times 100$	$P = \dfrac{\sum p_0 q_t}{\sum p_0 q_0} \times 100$
Simple Aggregate Price Index	**Paasche Quantity Index**
$P = \dfrac{\sum p_t}{\sum p_0} \times 100$	$P = \dfrac{\sum p_t q_t}{\sum p_t q_0} \times 100$
Laspeyres Price Index	**Fisher's Ideal Price Index**
$P = \dfrac{\sum p_t q_0}{\sum p_0 q_0} \times 100$	$\sqrt{(\text{Laspeyres Price Index})(\text{Paasche Price Index})}$
Paasche Price Index	**Value Index**
$P = \dfrac{\sum p_t q_t}{\sum p_0 q_t} \times 100$	$V = \dfrac{\sum p_t q_t}{\sum p_0 q_0} \times 100$

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II. STATISTICAL TABLE

Table 1 The Upper Tail Area Under the Standard Normal Curve	

Z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.5000	0.4960	0.4920	0.4880	0.4840	0.4801	0.4761	0.4721	0.4681	0.4641
0.1	0.4602	0.4562	0.4522	0.4483	0.4443	0.4404	0.4364	0.4325	0.4286	0.4247
0.2	0.4207	0.4168	0.4129	0.4090	0.4052	0.4013	0.3974	0.3936	0.3897	0.3859
0.3	0.3821	0.3783	0.3745	0.3707	0.3669	0.3632	0.3594	0.3557	0.3520	0.3483
0.4	0.3446	0.3409	0.3372	0.3336	0.3300	0.3264	0.3228	0.3192	0.3156	0.3121
0.5	0.3085	0.3050	0.3015	0.2981	0.2946	0.2912	0.2877	0.2843	0.2810	0.2776
0.6	0.2743	0.2709	0.2676	0.2643	0.2611	0.2578	0.2546	0.2514	0.2483	0.2451
0.7	0.2420	0.2389	0.2358	0.2327	0.2296	0.2266	0.2236	0.2206	0.2177	0.2148
0.8	0.2119	0.2090	0.2061	0.2033	0.2005	0.1977	0.1949	0.1922	0.1894	0.1867
0.9	0.1841	0.1814	0.1788	0.1762	0.1736	0.1711	0.1685	0.1660	0.1635	0.1611
1.0	0.1587	0.1562	0.1539	0.1515	0.1492	0.1469	0.1446	0.1423	0.1401	0.1379
1.1	0.1357	0.1335	0.1314	0.1292	0.1271	0.1251	0.1230	0.1210	0.1190	0.1170
1.2	0.1151	0.1131	0.1112	0.1093	0.1075	0.1056	0.1038	0.1020	0.1003	0.0985
1.3	0.0968	0.0951	0.0934	0.0918	0.0901	0.0885	0.0869	0.0853	0.0838	0.0823
1.4	0.0808	0.0793	0.0778	0.0764	0.0749	0.0735	0.0721	0.0708	0.0694	0.0681
1.5	0.0668	0.0655	0.0643	0.0630	0.0618	0.0606	0.0594	0.0582	0.0571	0.0559
1.6	0.0548	0.0537	0.0526	0.0516	0.0505	0.0495	0.0485	0.0475	0.0465	0.0455
1.7	0.0446	0.0436	0.0427	0.0418	0.0409	0.0401	0.0392	0.0384	0.0375	0.0367
1.8	0.0359	0.0351	0.0344	0.0336	0.0329	0.0322	0.0314	0.0307	0.0301	0.0294
1.9	0.0287	0.0281	0.0274	0.0268	0.0262	0.0256	0.0250	0.0244	0.0239	0.0233
2.0	0.0228	0.0222	0.0217	0.0212	0.0207	0.0202	0.0197	0.0192	0.0188	0.0183
2.1	0.0179	0.0174	0.0170	0.0166	0.0162	0.0158	0.0154	0.0150	0.0146	0.0143
2.2	0.0139	0.0136	0.0132	0.0129	0.0125	0.0122	0.0119	0.0116	0.0113	0.0110
2.3	0.0107	0.0104	0.0102	0.0099	0.0096	0.0094	0.0091	0.0089	0.0087	0.0084
2.4	0.0082	0.0080	0.0078	0.0075	0.0073	0.0071	0.0069	0.0068	0.0066	0.0064
2.5	0.0062	0.0060	0.0059	0.0057	0.0055	0.0054	0.0052	0.0051	0.0049	0.0048
2.6	0.0047	0.0045	0.0044	0.0043	0.0041	0.0040	0.0039	0.0038	0.0037	0.0036
2.7	0.0035	0.0034	0.0033	0.0032	0.0031	0.0030	0.0029	0.0028	0.0027	0.0026
2.8	0.0026	0.0025	0.0024	0.0023	0.0023	0.0022	0.0021	0.0021	0.0020	0.0019
2.9	0.0019	0.0018	0.0018	0.0017	0.0016	0.0016	0.0015	0.0015	0.0014	0.0014
3.0	0.0013	0.0013	0.0013	0.0012	0.0012	0.0011	0.0011	0.0011	0.0010	0.0010
3.1	0.0010	0.0009	0.0009	0.0009	0.0008	0.0008	0.0008	0.0008	0.0007	0.0007
3.2	0.0007	0.0007	0.0006	0.0006	0.0006	0.0006	0.0006	0.0005	0.0005	0.0005
3.3	0.0005	0.0005	0.0005	0.0004	0.0004	0.0004	0.0004	0.0004	0.0004	0.0003
3.4	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	0.0002
3.5	0.0002	0.0002	0.0002	0.0002	0.0002	0.0002	0.0002	0.0002	0.0002	0.0002
3.6	0.0002	0.0002	0.0001	0.0001	0.0001	0.0001	0.0001	0.0001	0.0001	0.0001
3.7	0.0001	0.0001	0.0001	0.0001	0.0001	0.0001	0.0001	0.0001	0.0001	0.0001
3.8	0.0001	0.0001	0.0001	0.0001	0.0001	0.0001	0.0001	0.0001	0.0001	0.0001
3.9	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
4.0	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000

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